Beam extraction studies at 900 GeV using a channeling crystal

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Luminosity-driven channeling extraction has been observed for the first time in a 900 GeV study at the Fermilab Tevatron. This experiment, Fermilab E853, demonstrated that useful TeV level beams can be extracted from a superconducting accelerator during high luminosity collider operations without unduly affecting the background at the collider detectors. Multipass extraction was found to increase the efficiency of the process significantly. The beam extraction efficiency was about 25%. Studies of time dependent effects found that the turn-to-turn structure was governed mainly by accelerator beam dynamics. Based on the results of this experiment, it is feasible to construct a parasitic 5–10 MHz proton beam from the Tevatron collider.

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I. INTRODUCTION

In the early 1990's a fixed target experiment was proposed for the Superconducting Super Collider (SSC) [1] to study heavy-flavor physics using a tiny fraction of the 20 TeV circulating beam extracted with bent crystal channeling. Conventional methods of beam extraction at such high energies pose problems with no obvious cost-effective solutions. For example, electrostatic septa cannot easily provide the larger momentum kicks required for future trans-TeV accelerators. Since the new extraction scheme proposed for the SSC was not a proven technique, E853 at Fermilab was designed to study the feasibility of this approach.

The goals of E853 were to extract $10^6$ 900 GeV/c protons/second with $10^{12}$ protons circulating in the Tevatron, to study the extraction efficiency, to show that the luminosity lifetime of the circulating beam was not adversely affected, and to investigate the backgrounds created at the two Tevatron collider experiments. Losses at these major collider experiments, CDF (one-sixth of the ring upstream for protons—see Fig. 1) and D0 (one-sixth of the ring downstream), had to be kept to a tolerable level. A central concern for the E853 operation was that losses be minimized so that the superconducting Tevatron magnets were not quenched.

There are significant constraints on where an inexpensive, parasitic extraction test can be placed within the Tevatron lattice. Any modification of the Tevatron vacuum system is expensive and requires rigorous attention to maintaining a very high vacuum. The C0 long straight section was chosen for E853 because it contained an existing 900 GeV abort system with an associated extraction line and dump that was not to be used in the 1994–1996 running period except at 150 GeV during collider injection tests. In addition there was free space along the abort beam line for instrumentation and cabling to a portakamp complex aboveground for electronics and data acquisition.

Reliable simulations were required to interpret the experiment and explore ideas for halo generation and future applications. A simulation needs to cover all of the accelerator physics issues involved as well as the physics processes associated with channeling and multiple scattering in the crystal. Simulations created for the experiment

II. EXPERIMENT

The apparatus for E853 was placed at C0 where there was an existing Tevatron abort line (see Fig. 1). The experimental layout at C0 is shown schematically in Fig. 2. Protons from the circulating beam were kicked or diffused outward to a bent crystal that deflected the particles upward. From there they traveled along a simple beam line through a quadrupole doublet that was part of the Tevatron lattice to two diagnostic counter stations. Measurements consisted of determining the count rate in the extracted beam line as a function of crystal alignment, strength of the beam halo excitation, and other parameters.

The bent crystal was installed 60 m upstream of the C0 straight section center at the location of one of the kicker magnets for the 900 GeV C0 abort system (B48). Because the proton beam was on the outside of the center line of the ring at B48, the crystal was placed on the outside of the ring (antiprotons were on the inside). The geometry is shown in Fig. 3(a).

The existing abort lattice was designed to provide an extraction system that would be fast (one turn) and clean so that it does not pose a problem for the string of superconducting magnets in the Tevatron [7]. The abort magnet string replaced by the E853 crystal consisted of four 1.8 m long kicker modules with peak fields of 3.7 kG and...
FIG. 2. Schematic of the channeling extraction experiment at C0. The bent crystal is on the outside of the ring and deflects protons up through the quadrupoles (Q) into the field-free region of the Lambertson magnets. Downstream of the C0 midpoint the extracted protons are detected in two air gaps containing scintillators, a scintillating screen, and a SWIC.

Extraction consists of two parts: a vertical kick into the field-free region of a string of Lambertson magnets, as shown in Fig. 3(b), and horizontal separation of the circulating beam from the extracted beam by the Lambertsons. In the Tevatron lattice missing half-dipoles at B48-3 and at C11 establish a three-bend magnetic dogleg and thereby provide an effective 4 mrad horizontal kick at B48 so that the abort line can clear the magnets at the downstream end of the straight section. The missing bend in the accelerator ring resulting from the removal of the half-dipole is supplied by the warm Lambertson magnets and C-magnets in the straight section itself. The field-free and field regions of the Lambertsons then provide the initial horizontal separation between the extracted and circulating beams. For E853 the 640 μrad crystal bend deflected the beam incident on the crystal up into the field-free region of the Lambertson magnets.

Since E853 was carried out parasitically to the collider program, it was not possible to optimize the accelerator lattice for channeling extraction. For example, it would have been desirable to have more dispersion at the crystal so that longitudinal noise excitation could have been carried out. The accelerator parameters are given in Table I for the two types of stores in which E853 had a study session:

![Diagram](image)  
**Table I.** Accelerator parameters for the two types of stores in which E853 took data. $D$ is the horizontal dispersion, $\epsilon$ is the one-σ normalized emittance, $\beta$ and $\alpha$ are the standard parameters describing the shape of the emittance ellipse, and $\nu_x$ and $\nu_y$ are the horizontal and vertical tunes of the accelerator. $x-p$ and $y-p$ are the horizontal and vertical positions of the protons at the crystal relative to the central orbit of the Tevatron.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Proton only</th>
<th>$\vec{p}p$</th>
<th>Units</th>
</tr>
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<td>6.66</td>
<td>π mm mrad</td>
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<td>$\beta_x$</td>
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<td>0.13</td>
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</tr>
<tr>
<td>$\alpha_y$</td>
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<td>0.10</td>
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<tr>
<td>$D$</td>
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<td>1.887</td>
<td>m</td>
</tr>
<tr>
<td>$\sigma_x$</td>
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<tr>
<td>$\sigma_y$</td>
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</tr>
<tr>
<td>$\nu_x$</td>
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<td>20.585</td>
<td></td>
</tr>
<tr>
<td>$\nu_y$</td>
<td>20.574</td>
<td>20.574</td>
<td></td>
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<tr>
<td>$x-p$</td>
<td>0</td>
<td>1.99</td>
<td>mm</td>
</tr>
<tr>
<td>$y-p$</td>
<td>0</td>
<td>-1.99</td>
<td>mm</td>
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<tr>
<td>$x-\vec{p}$</td>
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<td>-0.75</td>
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<tr>
<td>$y-\vec{p}$</td>
<td>0.75</td>
<td></td>
<td>mm</td>
</tr>
</tbody>
</table>
The basic technique was to move the crystal in to a pre-
determined horizontal location close to the beam (4.5 to
6\(\sigma_x\) from the beam center). The beam was then kicked
horizontally a number of times by a fast kicker at E17 (see
Fig. 1). At this distance from the crystal, the beam density
was so small that no beam was observed to interact with
the crystal on the first few kicks.

However, after several hundred turns following a kick,
the beam had grown in size as nonlinearities in the machine
gradually spread the beam to fill much of the phase space
mapped out by the betatron oscillation. After about six
such kicks, the beam size had grown by a factor of 1.7
in the horizontal plane and a factor of 1.2 in the vertical
plane (resulting from the horizontal/vertical coupling in
the Tevatron). In the kicks that followed, an equilibrium
state persisted in which the rising edge of the Gaussian
beam distribution led to a nearly constant loss of about
2 \times 10^9 protons/kick, and extraction by the crystal was
observed.

The second extraction technique was called “diffusion
mode,” relying on either natural or stimulated diffusion
during proton-only stores and \(\overline{p}p\) collisions parasitic to
collider operations. This diffusion was due to such effects
as beam-gas scattering, beam-beam interaction and tune
shift effects, magnetic field ripple, and imposed rf noise.
In this mode, the crystal was slowly moved into the tail
of the beam halo. As the crystal approached the beam,
the extraction rate rose rapidly, as illustrated in Fig. 4.
Movement of the crystal was halted when an extraction
rate adequate for the studies had been achieved. When
operating parasitic to collider operations, this mode did
not seriously affect the circulating proton beam lifetime.

Protons were steadily resupplied onto the crystal either
by natural diffusion, artificially applied rf noise, or \(\overline{p}p\)

![Figure 4](image)

**FIG. 4.** Extraction rate in the diffusion mode as the crystal was
moved in closer to the beam. \(X\) is the distance from the beam
centerline to the face of the crystal next to the beam.
collisions. The beam which did not channel on the first encounter with the crystal underwent multiple scattering and got another chance to enter the crystal on successive turns, if it did not interact in the crystal. The most effective instrumentation for beam measurement in this mode was the scintillation counter system set at voltage levels appropriate for single particle identification.

A horizontal damper located at F11 was also used in two E853 sessions to introduce rf noise in transverse phase space and thereby stimulate diffusion and increase the extraction rate. This characteristically decreased the beam lifetime substantially although it was still long enough for a typical study session. Significantly higher extraction rates were observed with the noise on. This approach could not be used for parasitic extraction owing to its destructive effect on the circulating beam.

III. APPARATUS

This section reviews the main components of E853. The operation of the Tevatron, which was at the heart of the experiment, has already been described. The other principal components of the apparatus were the channeling crystal with its associated goniometer and the diagnostic instrumentation to carry out the experiment. Both special instrumentation and the existing Tevatron diagnostics were required to study the circulating and extracted beams. Finally, data collection was provided by an on-line computer system as well as the extensive accelerator ACNET control utility.

A. Bent crystal operation

Channeling requires a well-characterized crystal, a device to bend the crystal, and a precise and flexible goniometer. These systems are discussed in the following paragraphs.

1. Crystal

The “dislocation-free” silicon crystal used for E853 was obtained from the Wacker Corporation after crystals from several sources were evaluated for dislocation density using a two-crystal x-ray diffraction spectrometer discussed in Baublis et al. [8]. The crystal had a diffraction linewidth of (4.5 ± 0.5) μrad which confirmed that it was dislocation free. For the experiment, several 39 mm long, 3 mm high, 9 mm wide crystals were prepared with different planar orientations.

The crystal used in the experiment was cut so that a (111) plane was aligned to within 1000 μrad of the crystal face. A more comprehensive view of the planar alignment for one of the crystals is shown in Fig. 6 of Baublis et al. The side facing the beam was polished to be optically flat within half a wavelength. The results of this process are illustrated in Fig. 7 of Baublis et al.

FIG. 5. Four-point crystal bender. An interaction counter below and downstream of the bender is illustrated schematically (not to scale).

2. Bender

A four-point bender was chosen for E853 to produce a uniform bend. A drawing of the bender with the crystal and alignment mirror is shown in Fig. 5. Note that the crystal had straight overhangs of 7.5 mm beyond the outer points of support for the bend. More details on the design aspect of the bender can be found elsewhere [9].

The crystal was prebent up through an angle of 642 μrad. The bend angle was set to within 5 μrad using two independent techniques: laser interferometry and autocollimation. A small mirror was carefully aligned with the top surface of the upstream end of the crystal prior to installation. The crystal was positioned in the Tevatron using survey monuments on the outside of the goniometer. That alignment was checked by autocollimation using the upstream reference mirror. The upstream top face orientation of the crystal was estimated to be within 150 μrad of the Tevatron beam based on the effect of refraction in the viewing window, 10 μrad surveying errors, and other factors.

Both the horizontal and vertical angle initial alignments in the accelerator were assisted greatly by relating the upstream and downstream ends of the two crystal surfaces (only 40 mm long) to the survey monuments external to the 1 m long goniometer tube using the Coordinate Measuring Machine of the Fermilab Silicon Detector Facility. This device has an accuracy of 2 μm globally, leading to an uncertainty of about 100 μrad in the angles of the crystal with respect to the external monuments. The optical techniques for measuring the external fiducials during installation in the accelerator are accurate only to 100 μm, implying an additional uncertainty of 100 μrad over the 1 m length.

3. Goniometer

For channeling to occur, the vertical angular orientation of the channeling crystal must be aligned with the beam angle. Since the Tevatron beam has a vertical angular divergence of 11 μrad in proton-only stores and the critical angle of the crystal at 900 GeV is 5.2 μrad, the crystal...
alignment must be within the order of 20 μrad for channeling to occur. A special goniometer was designed for E853 to position and align the crystal quickly inside the vacuum system of the Tevatron. Precision stepping motors outside the pipe at each end of the vacuum pipe allowed alignment of the crystal with 4 degrees of freedom (x, Θₜ, y, and Θₚ).

The crystal was mounted at the upstream end of a 1 m long beam pipe with articulating bellows at the ends. Because of the upstream location of the crystal the angular motion was provided solely by the downstream motors and the crystal turned around its own center. The motors produced step sizes of 2.5 μm that translated to 2.5 μrad in angle with the 1 m lever arm of the goniometer. The accelerator control system was used to control the goniometer. A schematic of the goniometer is shown in Fig. 6(a).

A horizontal retractor controlled by a fifth motor was used to move the crystal holder in and out of the beam. The crystal was completely outside of the Tevatron aperture when not in use. The retractor also preserved the crystal orientation over many excursions of the crystal holder out of the beam pipe with a reproducibility of 15 μrad. The retraction arrangement is shown in Fig. 6(b).

Extensive reproducibility studies of the goniometer motions were carried out. These were done for different load conditions to simulate the real conditions with the meter-long insert attached to the motion tables. The minimum step sizes on the x, y motion stepping motors and on the motor used by the retraction mechanism were verified using a high-resolution (1 μm) optical encoder. The backlash error was of the order of 3 to 4 μm.

B. Extraction line instrumentation

The instrumentation for beam detection and measurement was placed in two air gaps along the abort line. Eight plastic scintillation counters of various shapes and sizes were used to monitor the beam flux close to the crystal and along the extraction line. The operating voltages for single particle counting were determined with cosmic rays and beam coincidence studies. For diffusion mode the counters were operated as single particle counters. Count rates were limited to somewhat less than the bunch passage frequency (300 Khz for six bunches).

For the kick mode a significant fraction of the circulating beam was extracted down the abort line in the first few turns so that it was not possible to count individual particles. Typically 2 × 10⁹ protons were lost per kick. Assuming an extraction efficiency of 30% on the order of 10⁹ protons could come down the extraction line in a single rf bucket. This flux could saturate the counter itself or the analog to digital converter (ADC) used for charge integration. Kick mode voltages were set lower to avoid these problems. The scintillators acted as calorimeters and their pulse heights were recorded.

Three principal counter combinations were used. Two counters in the first air gap formed a coincidence called AG1. This was often placed in coincidence with a counter in the second air gap such as the one referred to as CAL. Interaction counters below and slightly downstream of the crystal were employed to monitor interactions of the beam with the crystal.

These interaction counters consisted of a pair of scintillators in coincidence with dimensions 10 × 10 cm². Typically they were placed about 1 m from the crystal at an angle of 25° to the beam. Since they were used only to monitor changes in the interaction rate as conditions changed during particular sessions, their specific geometry was not important. No effort was made to measure an absolute interaction rate.

In kick mode, ADC readings for the various counters were taken for the second revolution of the proton bunch around the ring after the beam was kicked (the beam was on the far side on the first turn after the kick). Typically several scintillator signals were also recorded for many turns with digital oscilloscopes.

Because the C0 abort line was routinely used for 150 GeV extraction of the entire beam during collider setup periods, the counters at the air gaps were mounted on horizontal linear motion stages in order to allow them to be removed remotely when not in use. A vertical finger counter (width = 1.6 mm) on the second air gap stage was used to study the horizontal beam width while a horizontal finger counter (height = 0.8 mm) was independently mounted on a vertical motion in the first air gap to measure the vertical profile. The ACNET control system was used to operate the stages.

The extracted beam was also monitored with a chromox fluorescent screen (from the Morgan Matroc Co.) at the first air gap. A conventional SWIC with 1 mm wire spacing in x and y already existed in the second air gap. In kick mode both of these devices provided information on
the beam size and position. The fluorescent screen and the
SWIC were not useful in the diffusion mode because there
was not a high enough flux of beam particles to produce
signals. The fluorescent screen was viewed with a CCD
camera connected to a video monitor and tape recorder.
Videotapes were used to look at time dependent effects
with scales greater than 15 ms in the kick mode.

The screen image of the beam was also captured and
stored with the help of a “frame grabber.” The images were
analyzed later to determine the beam distribution in both
the horizontal and vertical projections. Figure 7 shows
typical frame grabber views of the beam spot for the kick
mode. Despite problems with saturation and calibration,
the screen provided a useful visual tool to guide one during
the initial setup for crystal alignment. The fluorescent
screen was also useful in determining the extracted beam
position with respect to the aperture of the Lambertson
magnets.

C. Accelerator instrumentation

The characteristics of the circulating beam and the loss
rates at the collider detectors were measured using exist-
ing Tevatron diagnostics. Electromagnetic beam position
monitors in the accelerator ring continuously tracked the
position of each bunch of the circulating beam at many
points around the accelerator and were used to determine
the distance of the proton beam from the crystal. Resistive
wall monitors and dc current transducers tracked the total
circulating intensity. These signals, averaged over several
turns, were used to determine the total loss rate from the
beam, not just that resulting from the crystal. They were
also useful quantities for normalizing the extraction rate in
the diffusion mode.

Beam profile measurements in the Tevatron were done
with a system of three “flying wires” at E11 and E17. A
flying wire is a 30 μm diameter carbon fiber that moves
through the beam with a speed of ≈5 m/sec. The sec-
ondary particles from the interaction of the beam with the
filament are detected as a function of time using a scintilla-
tor telescope. This gives the beam intensity profile directly.

Vertical and horizontal beam profiles were taken in the
kick mode with the flying wires before and after beam
growth with the first six kicks. With the emittances deter-
mined at one location, it was straightforward to calculate
the beam divergences at the crystal knowing the relevant
lattice Twiss functions.

Loss rates at the collider detectors were measured us-
ing permanent counters located at B0 (CDF) and D0. For
ordinary Tevatron collider operations the circulating
beam was scraped until these count rates were below stan-
dard operating upper limits. Data from all these sys-
tems are available at E853 through the accelerator ACNET
system.
IV. CHANNELING BEHAVIOR

While E853 was the highest energy channeling measurement yet performed, it was undertaken to look at channeling extraction, not the fundamentals of the channeling process. Because the energy was high, the channeling critical angle was small, \(5.2 \mu \text{rad} \) at 900 GeV. As a consequence, it was difficult to measure the size of this angle directly. Nevertheless, information from E853 confirms that the channeling process continues to behave consistently in the TeV range.

A. Crystal angular alignment

1. Vertical angle alignment

For successful extraction the channeling plane of the crystal must be aligned with the circulating accelerator beam. The angular width of the \( \Theta_v \) scan (varying the vertical angle of the crystal) is determined by three factors. One is the channeling critical angle, another is the angular divergence of the accelerator beam, \( \sigma_{\theta_v} \), and the third is the impact of multiple passes through the crystal on the angular divergence of the beam halo.

At the crystal \( \sigma_{\theta_v} \) was typically \(18 \mu \text{rad} \) during collider-mode stores. The rms multiple scattering for one pass through the crystal was \(10.8 \mu \text{rad} \). Characteristically in the diffusion mode a proton passed through the crystal several times before it was properly aligned for channeling. The effective multiple scattering angle was proportional to the square root of the number of passes through the crystal.

The lower panel of Fig. 8 shows a typical crystal \( \Theta_v \) extraction curve in the diffusion mode during a collider store. Biryukov's simulation [3] predicts \( \sigma_{\theta_v} \) to be 21 to 24 \( \mu \text{rad} \) compared to 32 \( \mu \text{rad} \) measured in Fig. 8. Fitted values for various sessions ranged from 28 to 37 \( \mu \text{rad} \). The discrepancy between the simulation and experiment arises because the simulation took the beam divergence to be 11.5 \( \mu \text{rad} \), whereas the beam divergence in the collider mode was 18 \( \mu \text{rad} \) (see Table I).

In the kick mode, data were taken for the \( \Theta_v \) scan and other scans only on the first pass of the kicked bunch through the crystal (the second turn after the kick; see Sec. VII). Therefore, the \( \Theta_v \) curve should be narrower than in the diffusion mode because there was no multiple scattering. The upper panel of Fig. 8 shows a kick mode vertical scan gated on the second turn for which \( \sigma_{\theta_v} = 18 \mu \text{rad} \), illustrating the suppression of multipass multiple scattering. Because of the beam growth resulting from the kicks, this width was expected to be somewhat greater than 15 \( \mu \text{rad} \).

2. Horizontal angle alignment

Before the experiment began there was concern that the horizontal angle of the crystal might have to be aligned very accurately in the diffusion mode so that the edge was quite parallel to the beam. Fortunately, multipass extraction in the diffusion mode obviates this problem, since multiple scattering from the portion of the crystal projecting out into the beam scatters particles out to larger radii on later turns.

Beyond this concern there were several impacts of horizontal angular scans. As the crystal rotated in \( \Theta_h \) starting from a well-aligned angle (\( \Theta_h = 0 \)), either the downstream or the upstream end moved closer to the beam. For example, a 10 mrad change in \( \Theta_h \) moved both ends of the crystal by 200 \( \mu \text{m} \) in opposite directions. As a result of the end moving into the beam the interaction counter rate rose. This behavior is illustrated in Fig. 9. The time order of the data was from right to left. As \( \Theta_h \) decreased from its starting value of 8 mrad, the interaction rate is observed to decrease, because as the upstream end of the crystal moved out of the beam it was intercepting a region from which most of the particles had been removed at the previous angular setting, and diffusion had not yet had a long enough time to repopulate the void.
FIG. 9. Interaction counter rate with the background subtracted for a $\Theta_h$ scan in the diffusion mode. The downstream end of the crystal points out for positive $\Theta_h$. Note that the minimum of the curve is near $\Theta_h = 0$.

This effect was anticipated, for it had been observed that when the whole crystal was translated away from the beam by 200 $\mu$m, it took some minutes for the diffusing beam to reestablish a constant interaction rate. When the goniometer reached $\Theta_h = 0$, the downstream end of the crystal began to move into the beam and intercept increasingly repopulated regions as the angle continued to change; therefore, the interaction rate rose steadily.

We take the interaction rate to be proportional to the amount of beam incident on the crystal. Then the quantity of interest to plot as a function of $\Theta_h$ is the beam extracted divided by the background-subtracted interaction counter rate (see Sec. VI). This is shown in Fig. 10. The shape of the curve agrees well with Biryukov’s simulation. For $\Theta_h$ the half width at half maximum is of the order of 10 mrad, approximately 30 times wider than the $Q_y$ distribution (Fig. 8).

For the kick mode a uniform 20 $\mu$rad change in $\Theta_v$ was observed with the CCD camera over a 20 mrad change in $\Theta_h$ around $\Theta_h = 0$. This change was in line with the change predicted for crystal distortions resulting from the bender. As the downstream crystal end moved away from the beam to angles beyond 10 mrad there was a slight indication that the deflection was decreasing. For a 0.5 mm kick this effect should have become significant for $\Theta_h \gg$ 20 mrad.

**B. Extracted beam size**

The beam optics in the vertical plane of the extracted beam was point to parallel from the crystal to the air gap region so that the beam height was directly related to the critical angle. Because of the optics, the accelerator beam height contributed little to the extracted beam height. The vertical beam profile was measured with a 0.8 mm high finger counter in the first air gap. The smearing of the vertical beam height distribution because of the finite counter width was 0.8 mm/$\sqrt{8.5}$. Figure 11 shows the distribution for the most carefully measured finger scan. The vertical beam distribution gave a raw width of $\sigma_v = 0.32$ mm. Factoring out the finite counter width gives $\sigma_v = 0.25$ mm. The expected width based on the beam optics and the critical angle was $\sigma_v = 0.23$ mm.

Alternatively, one can calculate a value for the critical angle directly by noting that $\sigma_v = M_{12}\Psi_c$, where $\Psi_c$ is the critical angle, and $M_{12}$, the beam transfer matrix element from the crystal to air gap 1, was 41.3 m. Substituting the measured extracted beam height gives $\Psi_c = 6.0$ $\mu$rad, compared to the expected value of 5 $\mu$rad. The

**FIG. 10.** Comparison of the normalized extracted rate for a $\Theta_h$ scan (circles) to the extraction efficiency from the Biryukov simulation in diffusion mode (diamonds).

**FIG. 11.** Vertical profile of the extracted beam taken with a thin finger counter. Note the dechanneling tail extending below the main peak. The open circles have been multiplied by 20 to show the behavior of the dechanneling tail. The solid line is a Gaussian fit to the data in the peak region.
apparent good agreement may be fortuitous. While no error has been assigned, it would be dominated in part by uncertainty in the finger counter angular alignment, which would make the effective counter width greater than 0.8 mm. Rather, the point is that the vertical distribution was consistent with the magnitude of the critical angle.

Because of the optics, the horizontal beam distribution in the air gaps was dominated by the halo angular distribution that reached the crystal. The horizontal size of the source at the crystal was also quite small in the diffusion mode so that $\sigma_h = 132 \sigma_{\alpha h}$, where 132 m is the appropriate beam transfer matrix element.

Only three plausible horizontal distributions were measured because of time pressure and problems with the counter. A proton-only store gave $\sigma_h = 2.8 \pm 0.5$ mm while two colliding beam stores gave $\sigma_h = 1.1 \pm 0.2$ mm and $1.2 \pm 0.2$ mm. The vertical finger counter in air gap 2 was 1.6 mm wide. When the effect of the width is factored out, the horizontal width ranged from 1.0 to 2.8 mm which suggests values for the halo angular distribution on the crystal of 8 to 21 $\mu$rad. The lower value is consistent with the angular distribution based on multipass multiple scattering extraction.

C. Dechanneling

A flat dechanneling tail is clearly visible in the $y$ finger distribution in Fig. 11 and in the CCD images of Fig. 7. The tail is cut off on the left side of Fig. 11 by the steel of the Lambertson magnet. The percentage of the particles in the visible tail is 20% of the peak. Biryukov’s simulation [3] predicted 26 $\pm$ 2%. Given the complexity of the dechanneling process for the accelerator beam halo, the agreement between the experiment and the simulation is adequate.

V. EXTRACTION RATES

A principal purpose of this experiment was to study absolute extraction rates under various conditions. We have measured extraction rates under three conditions: extraction driven by natural diffusion during proton-only stores, rf noise-driven diffusion during a proton-only store, and luminosity-driven extraction during proton-antiproton stores.

Direct digital counting measurements of the beam extracted down the beam line required several corrections. The pair of counters in coincidence in the first air gap which counted the extracted beam was corrected for the 90% efficiency of the pair. Accidental coincidences were negligible because of the low rate of nonextraction backgrounds. Small corrections for multiple particles extracted from the same rf bucket which the scintillators would count as one particle were calculated by Poisson-statistics techniques and were empirically verified in three of the sessions by recording the pulse heights in each of the counters for 10000 events. In the worst case, this correction raised the extraction rate by 70%, but more typically was a 10% correction.

The finger counter distributions were used to make other small corrections for the ambient background and for the dechanneling tail, which was subtracted from the extraction rate, because in a real application of this technique this tail would not survive the rest of the beam line. This correction typically reduces the extraction rate 15%.

In a typical proton-only store, $10^{11}$ protons were circulating in six bunches. In this mode, the maximum extraction rate achieved was 200 kHz. Higher rates could have been achieved by moving the crystal even closer to the beam, but with only six bunches, a rate of 287 kHz corresponded to extracting on average one proton per bunch, and the counters could not count more than one particle per bunch.

To mitigate this limitation, a special store was arranged with $10^{12}$ protons circulating in 84 bunches. Additional diffusion was induced by transverse rf horizontal noise using the electrical damper located at F11, creating an rms diffusion rate at the crystal of 0.04 $\mu$m per turn. The extraction rate was greater than 450 kHz.

In the luminosity-driven stores, typically $10^{12}$ protons were circulating in six bunches. The maximum extraction rate achieved was 150 kHz. In this mode the limitation was the impact of particles scattered from the crystal in creating backgrounds for the operating collider experiments. Although the CDF experiment received no measurable background from the crystal, the D0 “lost proton” monitor was sensitive to scattering from the crystal. D0 was usually already running at 80% of the conservative upper limit set by that experiment before the crystal was moved close to the beam and reached the limit when the extraction rate was between 50 and 150 kHz.

This limitation was removed during a special store with 36 proton bunches and 3 antiproton bunches during which D0 was not taking data. There were $3 \times 10^{12}$ protons circulating, and an extraction rate of 900 kHz was achieved. The D0 lost proton monitor exceeded its upper limit by a factor of 1.5 before the crystal was inserted and exceeded the limit by a factor of 2 after the crystal was inserted.

During that same store, the extraction rate was also studied as a function of luminosity. Only six of the proton bunches were colliding with antiprotons. Colliding and noncolliding proton bunches were observed during the same counting interval by employing two gates triggered on different bunches. With a typical bunch luminosity of $0.4 \times 10^{30}$ cm$^{-2}$ s$^{-1}$ and typical circulating proton and antiproton bunch intensities of 4–6 $\times 10^{10}$ the extracted beam rate increased by factors of 4 to 8 for proton bunches that were colliding. The extraction rates resulting from collisions at CDF and at D0 were about the same. Further discussion is found in Sec. X.
VI. EXTRACTION EFFICIENCY

The principal motivation of this experiment was to explore the possibility of producing useful extracted beams during the collider operation without undue impact on collider experiments. To achieve such beams it is desirable for the efficiency to be as high as possible. Efficiencies of up to 15.4% were measured in a recent CERN 120 GeV experiment [10,11] and 18% at 270 GeV [12]. Recently a group at IHEP, Russia, working with an extremely short crystal has achieved efficiencies of the order of 45% [13].

“Efficiency” in this context is defined in two ways. One practical definition, which we call the “extraction efficiency,” is the rate of beam extracted into the extraction channel divided by the increase in the total circulating beam loss rate in the accelerator after the crystal was inserted. From an accelerator operation point of view, this is a practical definition, for it is the ratio of protons extracted to protons lost from the accelerator resulting from the crystal insertion. This definition was used in the CERN experiment.

Several effects contributed to this efficiency. The major contribution to lowering this efficiency was from protons that interacted with the crystal (12.9% of an interaction length) on one of their several passes through the crystal. A second contribution was from protons that were initially channeled, but then dechanneled after being bent through approximately 50 to 300 μrad. In this angular range, a proton is within neither the extraction channel aperture nor the circulating beam aperture and is intercepted by the Lambertson magnet steel or a collimator. A third contribution was from protons which were fully channeled but left the crystal through the beam-side surface of the crystal because they had a large negative horizontal angle, referred to hereafter as the “surface loss” contribution. On the other hand, unchanneled particles which only multiple scatter in the crystal rarely leave the aperture of the circulating beam, since the rms multiple scattering angle is 10.8 μrad, comparable to the angular divergence of the circulating beam.

While the numerator (the rate of beam extracted) was straightforward to measure, determining the change in the total loss rate from the accelerator was usually difficult. The loss rate was determined by doing a least squares fit to the slope of the circulating beam intensity versus time for 1 or 2 h before and after the crystal was inserted. The error in this slope was determined from the rms deviation of the data from the fitted line. The variation with time of the loss rates before the crystal was inserted, resulting from various instabilities in the accelerator, usually exceeded the difference between the crystal-out and crystal-in loss rates.

For instance, in one study session the fitted beam loss rates in the two half-hours just before inserting the crystal (in units of 10⁶ protons/s) were 0.0 ± 0.04 and 0.21 ± 0.04, and for the two half-hours after the crystal was fully inserted, 0.55 ± 0.12 and 0.15 ± 0.10. In cases such as the above where the fluctuation in the loss rate as a function of time exceeded the errors assigned from the rms of the overall fit, the errors in the overall fit to the 1 or 2 h period were adjusted upward to be consistent with the fluctuations.

No successful measurements of this type were obtained, but the data can be used to set 90% confidence level lower limits on the extraction efficiency (see Table II). To determine this lower limit on the efficiency, a 90% upper limit on the change in loss rate was calculated using the formula [14]:

\[ \delta L(90\%) = \delta L(\text{measured}) + 1.282 \times dL \]

where \( \delta L \) is the change in loss rate and \( dL \) is the error in the change in loss rate. The error in the extraction rate was negligible compared with the error in the loss rate. The values varied from session to session, a result of the fact that while the upper limit in the change of the loss rate was quite similar in all sessions, the extraction rate varied considerably. A complete summary of the raw data is contained in Ramachandran’s thesis.

A second way to measure the efficiency was to compare the number of protons that interact with the crystal when its vertical angle is not aligned to the beam with the number that interact when it is correctly aligned for maximum channeling. Fewer interactions are observed when the crystal is well aligned with the beam because fewer protons interact with nuclei when a significant fraction of the beam incident on the crystal is channeled. This is called the “channeling efficiency” and is defined as the difference between the aligned and unaligned interaction counter rates, divided by the unaligned rate.

The surface loss mentioned above does not lower this efficiency, and the dechanneling losses contribute only partially (once a proton has dechanneled after channeling through part of the crystal, it has less than 12.9% probability of a nuclear interaction). Thus this efficiency is expected to be slightly higher than the extraction efficiency.

A model for the ratio of these efficiencies can be constructed. Of the total number of particles, \( N_{\text{tot}} \), incident on the crystal (sometimes several times because of the multipass phenomenon), their ultimate fate falls into three

<table>
<thead>
<tr>
<th>Session number</th>
<th>Type of store</th>
<th>90% CL lower limit</th>
<th>Extr. rate</th>
<th>( \delta L )</th>
<th>( dL )</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>P</td>
<td>0.27</td>
<td>0.213</td>
<td>0.56</td>
<td>0.18</td>
</tr>
<tr>
<td>18</td>
<td>P</td>
<td>0.23</td>
<td>0.053</td>
<td>0.12</td>
<td>0.09</td>
</tr>
<tr>
<td>20</td>
<td>L</td>
<td>0.04</td>
<td>0.031</td>
<td>0.58</td>
<td>0.13</td>
</tr>
<tr>
<td>21</td>
<td>L</td>
<td>0.08</td>
<td>0.055</td>
<td>0.50</td>
<td>0.15</td>
</tr>
<tr>
<td>22</td>
<td>L</td>
<td>0.17</td>
<td>0.030</td>
<td>0.014</td>
<td>0.13</td>
</tr>
<tr>
<td>23</td>
<td>L</td>
<td>0.41</td>
<td>0.048</td>
<td>0.018</td>
<td>0.08</td>
</tr>
<tr>
<td>24</td>
<td>L</td>
<td>0.15</td>
<td>0.043</td>
<td>0.49</td>
<td>0.22</td>
</tr>
<tr>
<td>25</td>
<td>L</td>
<td>0.07</td>
<td>0.035</td>
<td>0.19</td>
<td>0.25</td>
</tr>
<tr>
<td>28</td>
<td>L</td>
<td>0.20</td>
<td>0.047</td>
<td>0.14</td>
<td>0.07</td>
</tr>
</tbody>
</table>

TABLE II. Measured lower limits for the extraction efficiency. In column 2, “P” means “proton only” and “L” means “luminosity driven.” \( \delta L \) and \( dL \) are explained in the text. CL, \( \delta L \), and \( dL \) are in units of 10⁶ p/s.
categories: those extracted, \( N_{\text{ext}} \); those interacting with the crystal, \( N_{\text{int}} \); and those intercepted by an accelerator collimator, \( N_{\text{coll}} \), after either dechanneling or large amounts of multiple scattering. When the crystal is very misaligned from the optimum channeling angle, all the particles interact with the crystal (ignoring for the moment the possibility that particles multiple scattered in the crystal are intercepted by a collimator).

Using the above definitions of extraction efficiency, \( EE \), and channeling efficiency, \( CE \), it is straightforward to show, \( CE = EE(1 + N_{\text{coll}}/N_{\text{ext}}) \). One then needs a model for the factor \((1 + N_{\text{coll}}/N_{\text{ext}})\). To first order, it is expected that those which centripetally dechanneled (which occurs entirely in the first 64 \( \mu \text{rad} \) of bending) or did not channel will remain in the aperture of the accelerator and reencounter the crystal on a later turn. However, those that dechannel in the angular range 60 to 580 \( \mu \text{rad} \) are expected to intercept a collimator. It is observed that the dechanneling tail is 20% of the extracted beam in the angular range 290 to 590 \( \mu \text{rad} \). Extrapolating linearly (not necessarily a correct assumption) to the angular range 60 to 580 \( \mu \text{rad} \), a value of 1.35 for the factor \((1 + N_{\text{coll}}/N_{\text{ext}})\) is obtained.

In order to do a better job of estimating the real effects of the collimators, a fast Monte Carlo program was written which simulated both types of dechanneling, calculated the probability of an interaction in the crystal for unchanneled and dechanneled particles, and added Gaussianly distributed multiple scattering angles for those which did not interact. These particles were then traced to the three critical collimators used to scrape the beam during the collider mode. The above factor was found to vary from 1.2 to 1.4, depending on the setting of the collimators and the model used to extrapolate the angular distribution of the normal dechanneling to the region where the tail was invisible. In this model the number of particles intercepted by collimators after multiple scattering in the crystal when the crystal was not aligned to the optimum channeling angle was not negligible (typically 15%).

In operation, the interaction counters were also sensitive to fluctuations arising from such effects as small horizontal deviations of the circulating beam. Some of these effects could change in an unpredictable way in the time it took to do a typical scan. For example, Fig. 12 shows both the extracted beam and the interaction counter rate as functions of \( \Theta_{y} \). The time ordering of the points in the scan is from right to left. Note that the interaction rate is considerably higher off peak to the right than to the left and is falling with time. In this case the time dependence is understood: the scan was begun immediately after the crystal had been inserted to 5 mm from the beam, and it took several minutes for the rate of the beam incident on the crystal to decrease to an equilibrium rate.

To mitigate such a possible time dependence, the best measurements were obtained by moving the crystal quickly back and forth from an aligned to a very unaligned vertical angle. An example of such data is shown in Carrigan et al. [6]. In all such measurements the crystal was moved quickly back and forth between three positions several times: aligned for maximum channeling, very unaligned at an upward angle, and very unaligned at a downward angle. The interaction rate was averaged at each angle, and errors determined from the rms deviation of the data from the mean. A weighted average was taken of the two off-peak values for use in the calculation of the channeling efficiency.

A background was also subtracted from the measured interaction rate. Experience showed that as the crystal was moved from its fully retracted position, the interaction rate increased as soon as the crystal was within the aperture of the accelerator, long before any crystal extraction was observed, and remained constant until the onset of extraction. This background was probably the result of a low-intensity, diffuse halo intercepting the large holder mass. (The active cross section of the holder was on the order of 10 times the cross section of the crystal.) This background varied from 6% to 36% of the off-peak interaction rate when the crystal had been fully inserted for maximum channeling, depending on the session, but was quite constant during a session. An error estimate for the background was made based on the rms deviation of numerous measurements of the background from the mean. This estimate was then propagated through the calculation of the efficiency.
The channeling efficiencies resulting from these measurements are shown in Table III. The efficiency need not be the same from session to session (for example, the collimator settings were different in each session, and distance of the crystal from the beam differed), but should be the same for different on/off scans during the same session. Therefore, weighted averages are shown in Table III for sessions 28 and 30. In fact, the weighted averages of the three sessions are remarkably similar, despite the fact that one of the three sessions was a proton-only fill in which the collimators were out of the beam.

Biryukov’s simulation [3] predicted an extraction efficiency of 43% for a crystal with an amorphous layer of 1 μm and 45% for a perfect crystal. The same simulation program reports a value consistent with the efficiency measured at 120 GeV at CERN [15]. Using the factor 1.3 mentioned above relating the extraction and channeling efficiencies, our typical measured channeling efficiency of ~30% leads to an extraction efficiency of ~23%.

One can also calculate channeling efficiencies using the exact same methodology with the data from the Θν scans, but a choice must be made about which points to call “on peak” and “off peak.” This was done using the plot of the extracted beam versus Θν. This approach has been discussed in Ramachandran’s thesis [5]. These results are not as credible as those of Table III, for in any of these scans, there may have been an unknown time dependence in the interaction rate resulting from other changes in the accelerator.

It would have also been interesting to measure the extraction efficiency in the kick mode. In this case the denominator (the number of protons lost from the circulating beam after each kick) was easy to measure, for in these proton-only fills, the kicks were nearly the only source of loss, and amounted to typically $2 \times 10^9$ protons/kick. However, it was very difficult to measure the numerator, the number of protons extracted following each kick. This intensity range, $10^9$ protons/kick, was too low for the toroid or SWIC to function. Attempts to calibrate the pulse height of the counters, operating at reduced voltage in the “calorimeter mode,” and to calibrate the CCD using aborts of the entire circulating beam were not successful because of the difficulty in injecting and measuring such small amounts of the circulating beam.

### VII. TIME DEPENDENT AND BEAM HALO EFFECTS

A wide variety of time dependent and beam halo effects were observed in the course of E853. Characteristic time constants ranged from tens of microseconds to many seconds. Some time dependent effects were inextricably related to the nature of channeling such as multipass processes where some fraction of the beam on an incorrectly aligned crystal scattered to an aligned angle on a later turn. The significance of multipass extraction has been discussed by Biryukov [16] and Taratin et al. [17]. It was first observed experimentally at CERN [18]. Other effects such as the behavior of the extracted beam rate as a function of crystal motion in and out of the beam were more directly related to accelerator beam properties. Twenty to forty turns after a kick, nonlinear effects entered. Nonlinear effects were particularly significant for the beam halo extracted by the crystal. These effects cannot be easily modeled with simulations but are nevertheless interesting and are discussed in this section.

As noted earlier, E853 data were taken in two modes, kick and diffusion. In the kick mode an individual bucket was kicked onto the crystal. In the diffusion mode some of the beam halo diffused out to larger distances because of such effects as beam-gas scattering and magnet ripple. A special case, rf noise, is discussed in a later section.

The following subsections discuss the kick mode behavior, beam halo effects observed through crystal and collimator motion, and oscillations and modulations.

#### A. Kick mode

The major time structure in the first ten to twenty turns in the kick mode was dominated by linear beam dynamics and multipass extraction. Because of the accelerator phase advance between the kicker magnet at E17 and the crystal at B48, on the first turn following the kick the beam had moved away from the crystal (illustrated in Fig. 3 of Ref. [4]). On turn 2, and again on turn 7, the beam was at maximum amplitude towards the crystal. Sizable extraction was expected on turns 2 and 7. On turn 2 particles that were not within the critical angle multiple scattered to create a halo around the core. Extraction occurred on the turns in between 2 and 7 only when the beam that was not channeled in turn 2 multiple scattered to a different vertical angle and then returned to encounter the crystal with the correct angle on a later turn. This process has been successfully modeled in simulations prepared by Biryukov [3] and Bogacz et al. [2].

<table>
<thead>
<tr>
<th>Session number</th>
<th>Type of store</th>
<th>Channeling efficiency</th>
<th>Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>27</td>
<td>L</td>
<td>0.24</td>
<td>0.08</td>
</tr>
<tr>
<td>28</td>
<td>L</td>
<td>-0.06</td>
<td>0.20</td>
</tr>
<tr>
<td>28</td>
<td>L</td>
<td>0.41</td>
<td>0.23</td>
</tr>
<tr>
<td>28</td>
<td>L</td>
<td>0.57</td>
<td>0.16</td>
</tr>
<tr>
<td>28</td>
<td>wt. ave.</td>
<td>0.35</td>
<td>0.11</td>
</tr>
<tr>
<td>30</td>
<td>P</td>
<td>0.32</td>
<td>0.11</td>
</tr>
<tr>
<td>30</td>
<td>P</td>
<td>0.33</td>
<td>0.15</td>
</tr>
<tr>
<td>30</td>
<td>wt. ave.</td>
<td>0.32</td>
<td>0.09</td>
</tr>
</tbody>
</table>
The in-between turns are called “wrong side” turns, in contrast with “right side” turns such as 2 and 7. As would be expected, the detailed microstructure of the turn-to-turn variation was quite sensitive to the accelerator tune. This was also observed experimentally for tune changes in different sessions. Indeed, information on the microstructure was more indicative of tune changes than underlying physics related to channeling.

Figure 13 illustrates the behavior for the actual data and the Bogacz et al. simulation for the first 23 turns (about 400 μs). In this time domain before nonlinear effects become significant the extraction data rate based on the pulse height in a scintillator is reasonably modeled by the Bogacz simulation program except that extraction persists longer than predicted. Not surprisingly, the detailed pattern from the Bogacz simulation is tune sensitive.

Figure 14 shows the extraction pattern for a longer period (200 ms or 10,000 turns) for the large, right side turns. The measured initial total decay time ranges from 0.6 to 2.5 ms. In that period the signal decreases by 10%–60% for different kicks. Short values for this decay are more in line with the Bogacz simulation. It is difficult to produce $1/e$ times of less than 0.9 ms with the Biryukov simulation. Under somewhat artificial conditions the Biryukov simulation can generate time constants greater than 2.0 ms. Changing the interaction length and the horizontal kick by substantial amounts produces less than a 20% change. Changing the horizontal misalignment by 10 mrad can double the decay time.

A related issue is how long it took to reach equilibrium when the crystal was vertically misaligned. Multiple scattering resulting from multiple passes through the crystal is the underlying mechanism for this effect. Figure 15 shows the time distribution for 38 turns after a kick for
a −60 μrad misalignment. Data sets were also obtained for −40 and −20 μrad misalignments.

The highest right side turn data (circle with an x) has been fitted with an exponential form. The form (dictated by available fitting routines) also effectively incorporates a time before any beam is extracted. At −60 μrad no beam appeared for several turns. The rise time was 170 μs or 8.5 turns. The asymptotic extraction signal was about 70% of the on-peak case. At −40 μrad, the initial delay was still several turns and the time constant was 120 μs. The asymptotic signal reached the on-peak value.

A naive picture gives some insight into the process. On every pass through the crystal (approximately every other turn) the particle was scattered 10 μrad by multiple scattering. To change by 60 μrad required on average 6² passes or 72 turns to full equilibrium while 30 turns were actually needed to get to 90% of the asymptotic value. Part of this difference was probably due to the effect of the beam divergence that was already 14 μrad after six kicks and continued to grow with each successive kick. With beam divergence and multiple scattering the time constant should go as \( \Theta_n^m \) where \( 1 < n < 2 \) and \( \Theta_m \) is the misalignment angle. The Biryukov simulation reproduces the general features of the data but the simulation time constants are roughly twice as long (200 μs at 40 μrad and 400 μs at 60 μrad) and the pattern is not as smooth as the data. A wider effective accelerator angular divergence than used in the simulation might have led to shorter times.

Another related subject is the time for a wrong side turn to come out at the same rate as a right side turn. This equilibrium is probably a result of nonlinearities in the accelerator lattice. Observationally the amplitude of wrong side turns remained small for 20 turns and then increased and came into equilibrium with the right side turns with a time constant comparable to the initial fall time for right side buckets. This is illustrated in Fig. 16. Neither of the simulations reproduces this feature since nonlinearities were not included. After several hundred turns in the Biryukov simulation the wrong side turns remain small with no discernible pattern. The experimental data have been fitted with an exponential distribution coming into equilibrium with an asymptote. An effective initial delay before a signal of about 350 μs (18 turns) was followed by a rise with a time constant of 520 μs.

A second interesting feature appears in Fig. 14. This is a 10 ms period where the extracted rate slowly changed. The envelope decreased slowly at first and then more quickly. The initial slow portion extended for on the order of 20 ms. The time constant to the 50% point was 30 to 50 ms. The data hint that this might have been mixed in with some sort of 30 to 50 ms peak-to-peak oscillation (see later discussions under oscillations). Neither of the simulations shows this effect. Again, a plausible suggestion for a driving mechanism is a nonlinear effect in the accelerator.

There were also effects extending out to many seconds after a kick. These were observed using video recordings at an effective rate of 60 frames/second with a CCD camera monitoring the scintillator screen in the extracted beam line. Three types of beam spot pictures were observed. One was the first frame corresponding to the first 16 ms of Fig. 14. This was typically followed by several frames of decreasing intensity corresponding to the decay portion of Fig. 14. A third set of pulses was observed at times well separated from the initial kick interspersed with many blank frames. Since the CCD-scintillator system was nonlinear it was not possible to make more than a qualitative judgment of the pulse intensity.
The number of these pulses versus time summed over several kicks is shown in Fig. 17 for all pulses (X’s) and for the lowest intensity ones (open circles). Note that this distribution is for the number of separated pulses, not the number of particles down the beam line. This distribution measures some convolution of the effect of small perturbations long after the kick with the available halo generated by the kick that has not yet been scraped. The distribution dies with a time constant of 0.8 s. After 5 s there is an almost flat spectrum of very small pulses.

B. Beam halo effects

Several E853 observations relate to the character of the circulating beam halo. The effect of retracting the crystal or a collimator a small distance sheds light on the diffusion rate of the halo. This rate is related to the beam halo phase space density and nonlinear effects in the accelerator system. Likewise, the number of kicks required to move the beam out to the crystal or “grow” the beam is an indicator of the halo density. Moving the crystal or a collimator generated related information. When the crystal was moved in there was an initial quick beam rise that died over a minute or so followed by a sustained rate that could persist for hours.

Unperturbed beam lifetimes in the Tevatron are quite long. For E853 typical proton beam lifetimes ranged from 70 to 90 h, while the luminosity lifetimes were 11 to 18 h. Because diffusion rates were long and data collection time was short, little data were taken where the incremental retraction of the crystal was small enough to produce a noticeable effect and the time interval before the next disturbance was long enough. Figure 18 shows the best information available from a diffusion session in the collider mode. After a 200 μm retraction the count rate dropped by a factor of 4 and then increased with a time constant of 2.2 min. Weaker information for a 50 μm retraction shows an initial drop of a factor of 2 followed by a rise with a time constant of ~15 s. Based on this information it is difficult to speculate on whether the time constant is linear or goes with the square of the retraction distance.

Collimator effects were also studied. The effect of the positioning of the three scraper collimators at D17 and A0 used to protect the collider experiments from the beam halo was clearly interwoven with a crystal position. When the crystal was effectively closer to the beam than the collimators the situation was different than when the crystal was shadowed by the collimators and the diffusing beam was mostly lost on the collimators. For example, a 5 mm retraction of the crystal (well outside the collimators) lowered the rate precipitously, and even after 20 min there was no sign of an increase.

In three study sessions the collimators were retracted almost simultaneously in small steps (typically 50 μm) near the end of the sessions by total amounts that varied from 0.5 to 1.2 mm. In all cases the extraction rate rose, but the rate of rise as a function of the collimator position varied. This may be a result of the fact that the collimators did not have the same initial settings in the three sessions. In a study with a total motion of 0.5 mm and the crystal 5.5 mm from the beam center the normalized extraction rate of rise was a factor of 5 per mm of collimator opening (normalized to the rate at the initial collimator positions), while in two later sessions with crystal-beam separations of 5.3 and 5.5 mm the rate of rise per mm was in the 1–1.5 per mm range. A plot of the extraction rate as a function of the collimator position for one of the latter sessions is shown in Fig. 19. The data are satisfactorily represented with a linear fit. In the three sessions the D0 proton loss rate rose by 5% to 20% as the collimators were opened.

FIG. 18. Extraction rate as a function of the collimator position for one of the latter sessions is shown in Fig. 19. The data are satisfactorily represented with a linear fit. In the three sessions the D0 proton loss rate rose by 5% to 20% as the collimators were opened.
Studies of the time to reach equilibrium after a collimator move were complicated by relatively quick collimator changes with a few measurements taken between adjustments. The time required to adjust the three collimators (on the order of 10 s) was also a limitation. Fast time plots and counting rate information indicated an initial fast rise of the count rate in less than 30 s, and perhaps much less. Information is available on only one relatively long quiescent period after a collimator move. Twenty minutes after completing a collimator moving session that had lasted 13 min the rate had risen by 30% (4 times the estimated standard deviation of the measurement).

Somewhat related information is provided by measurements of the number of kicks required to move the edge of the beam out to the crystal so that the asymptotic rate was reached. Typically it took 5–7 kicks to grow the beam. Figure 20 shows the behavior as a function of the kick number for a typical case when the crystal to beam center distance was 3.54 mm. The asymptotic rate was reached in five kicks. In a case with the crystal 4.5 mm from the beam it took ten kicks to reach the asymptotic rate.

Another related parameter is the time to reach an equilibrium extraction rate after the crystal was moved in. Normally there was only a short time interval available for analysis after the crystal was moved (typically 1–2 min) before some other change was made. Since equilibrium times were short, only data gathered starting a few seconds after a move could be used. A measure for the relaxation rate was obtained by fitting a linear slope to the extraction rate as a function of time to get \(-\frac{1}{T_e}\) which is equal to \(\frac{1}{T_e} = \frac{\partial R}{\partial t}\) (\(T_e\) is the time to approach equilibrium and \(R\) is the extraction rate). A typical value of \(\frac{1}{T_e}\) was \(0.15 \pm 0.03 \text{ min}^{-1}\). This means the rate dropped by 15% in a minute. The error bar is based on the uncertainty in clock time for the measurements (0.33 min).

The value of \(1/T_e\) at various distances from the beam and in various study sessions varied from 0.03 to 0.4 \text{ min}^{-1}. The equilibrium time seemed to shorten as the crystal was moved in.

After the initial rapid fall discussed above the rate decreased with a time constant \((1/e)\) between 0.5 and 5 h under a variety of operating conditions. Typically there is no statistical difference between a linear and an exponential fit to these long-term halo decays.

**C. Oscillations and modulations**

In the course of E853 several different phenomena appeared that were initially ascribed to some sort of oscillatory behavior. The possibility of oscillations with periods on the order of milliseconds was investigated and none were found.

The possibility of extracted beam modulation resulting from the Main Ring was also investigated. Initially there was concern that magnetic fields from the Main Ring or its power busses would produce Tevatron orbit perturbations large enough to modulate the extraction rate. The possibility of Main Ring oscillations was studied in the kick mode by looking at the number of pulses seen in the CCD camera long after the kick as a function of time in the Main Ring cycle. Figure 21 shows this distribution summed over the Main Ring cycle for several kicks. No statistically significant peaking in the distribution of the pulses was observed.

One oscillation-like behavior was observed in kick mode studies. It is illustrated in Fig. 14. This behavior showed wide variation from kick to kick. For example, the period between peaks varied from 25 to 75 ms. These oscillations were overlaid on the exponential decay of the signal after

![FIG. 20. Extraction rate as a function of the kick number. Characteristically it took five to seven kicks to reach the equilibrium rate. The extraction rate is normalized to the full extraction rate after the kicks.](043501-17)

![FIG. 21. Number of pulses long after a kick as a function of the time within the Main Ring cycle (summed for several kicks). There is little indication of any significant effect of the Main Ring cycle.](043501-17)
a kick. Only a few maxima were observed because the scope trace was only 200 ms long. As a result it was difficult to draw a conclusion. If this was an oscillatory effect it might have been related to synchrotron oscillations with a characteristic frequency of 39 Hz at 900 GeV or a subharmonic of the 60 Hz power.

VIII. RF-DRIVEN EXTRACTION

The impact of a transverse rf noise signal generated by the horizontal damper located at F11 was tested during two sessions. Betatron motion was excited by noise applied to the 6.4 cm gap of the 1.35 m long horizontal damper. The noise spectrum was centered at the betatron frequency and had a bandwidth of 1 kHz. The effect of turning the rf on or off was almost immediate and had a significant effect on the extracted beam. It was so significant that these tests were complicated by saturation problems in the larger principal counters even in a special proton-only store with 84 rather than 6 circulating bunches.

The smaller finger counters showed little or no evidence of saturation and also had a low background rate with noise off. Figure 22 illustrates the behavior of the crossed finger counter coincidence with increasing rms rf voltage for a crystal to beam separation of 3.94 mm. The curve shows a fit to the data of the form \( R = 15.2 \times V_{rf}^2 + 22 \) where \( R \) is the count rate and \( V_{rf} \) is the rms rf voltage. A \( V^2 \) dependence is expected from an analysis of the equations of motion in action-angle variables [19].

The possibility that accidental coincidences contributed to the crossed finger rate was studied. Accidentals were found to contribute 1.5% at a low \( V_{rf} \). This percentage should increase as \( V_{rf}^2 \) and was 12% at the highest voltage shown on Fig. 22. Accidentals were subtracted from Fig. 22.

In spite of the saturation problems it is still possible to make interesting estimates of upper limits on the time constants for rf changes. When the rf signal increased, the count rates (typically taken several times a minute) rose immediately, suggesting the rise time was less than a minute. Fast time plot information on rate meters rose within a 10 s period and probably somewhat more rapidly, suggesting a time constant \((1/e)\) of 2–3 s for \( V_{rf} = 4.5 \) V on the rf damper. This voltage should have resulted in a scattering angle of \( \Theta = 4 \times 10^{-3} \) µrad and a jump at the crystal of 0.04 µm/turn. If this was a linear process with a linear growth with time it would have taken 1.5 s for a particle to move out to 5\( \sigma_x \). This naive calculation is meant to show only order of magnitude agreement with the observations, for the correct model for this stochastic process is complicated by factors such as the beam halo distribution.

The fast time plots also provided information on the effect of turning off the rf damper or turning the rf down. When the damper was turned off from \( V_{rf} = 4.5 \) V the extracted beam rate decayed over a 15 s time period with a time constant \((1/e)\) of about 10 s.

IX. LUMINOSITY-DRIVEN EXTRACTION

During the first E853 parasitic collider session the channeled flux was substantially higher than earlier dedicated sessions with the crystal at the same relative distance from the beam. A principal candidate for a driving mechanism was the effect of interactions at the luminous regions for the two collider experiments on the halo of a proton bunch. In one picture of this process the halo is fed by proton-antiproton elastic collisions. The effective scattering target that feeds the halo is the antiproton current \( (I_p) \) times the geometrical part of the luminosity \( L \) so that the halo feed term is a geometrical factor times \( I_pL \). The halo is proportional to the luminosity and the extracted beam rate is then proportional to the luminosity. Another mechanism that can feed the beam halo is the effect of nonlinear fields from beam-beam interactions. In that case the halo may depend on the bunch length and also be proportional to higher powers of the beam currents. The actual situation could depend on machine conditions and be a mix of several processes. For this investigation using the Tevatron collider in operation for particle physics it was not possible to unfold these mechanisms.

Since several factors influenced the extracted beam rate it was interesting to isolate luminosity from other effects. The equivalent in a fixed target experiment would be a target in/target out measurement. Several approaches were considered: (1) changing the arrival times of the proton and antiproton bunches at the interaction points so they did not collide (cogging), (2) displacing the antiproton beam at the interactions points, and (3) eliminating some of the antiproton bunches and thereby removing the “target.” All of these required semidicated running. Cogging was tried several times and led to ambiguous results because the proton beam invariably moved transversely at some

![Fig. 22. Finger counter coincidence rate as a function of rf damper voltage. The errors are based on interpoint variation. The curve is a fit to the data.](image-url)
point during the exercise due to lattice dispersion. No opportunity arose to try displacing the antiproton beam, but it might not have worked for the same reason cogging did not work. The approach that worked was to run with a special store with 36 proton bunches of which only six were colliding with three antiproton bunches.

The test of the luminosity-driven process was to first check that the beam extraction rate was substantially higher with a gate timed to overlap a colliding bunch than it was for a noncolliding bunch. Then the relationship of the count rate to the bunch luminosity was investigated.

The Tevatron operated at 900 GeV with the separators on for this store. The 36 proton bunches were spaced in groups of twelve distributed evenly 1/3 around the ring. The individual proton bunches in groups of 12 were each separated by 395 ns. Three bunches of antiprotons were circulating spaced as though they were in one group of twelve with positions A1, A5, and A12 filled. This resulted in six sets of bunches colliding at the interaction regions shown at the top of the columns in Table IV.

Data were recorded for the number of protons and antiprotons in each bunch as well as the transverse size of the bunches. Typically the number of protons in a bunch was $50-70 \times 10^9$ and the number of antiprotons was $40 \times 10^9$. Information was also available on the population numbers for nearby satellite bunches. Some D0 luminosity information was also recorded. There were some problems in recording information on luminosities and several other ACNET variables because the complicated 36 on 3 collision pattern resulted in the need to reset many ACNET timing signals. As a result some information on luminosity was lost.

With the exception of P25 the transverse bunch widths ($\sigma$) were all on the order of 0.5 mm (at the flying wire location) for this session. For P25 the bunch width was 0.65 mm. No data are available on the horizontal antiproton bunch width.

Two sets of measurements were taken. In the first set an effective gate consisted of three windows each of 470 ns spaced evenly over a turn. Two such independent gates were used. The gates were broader than the spacing between two bunches because it was sometimes difficult to set the Tevatron timing signal to better than 100 ns. (In several cases the gates were set to nominally noncolliding time values that were later shown to collect colliding bunches.) Typically one of the two gates was set on a colliding bunch and the other on a noncolliding bunch.

With this arrangement collisions were detected that resulted from both the B0 and D0 interaction regions (set 1). Halfway through the measurements a different arrangement was adopted with only one window (rather than three equally spaced ones) to see the individual effects of D0 and CDF (set 2).

During the course of these two sets of measurements the ungated count rates dropped steadily. Both the colliding and the noncolliding bunch rates exhibited this behavior. This suggests that the count rate drop was not an effect related to luminosity. As a result of this drop in rate it was necessary to move the crystal 300 $\mu$m farther in toward the beam at the end of the first set (from a crystal to beam separation of 5.58 mm initially) to increase the instantaneous count rate at that time by a factor of 1.82. The time dependence for the first set of measurements was exponential with a lifetime of 1.5 h ($1/e$). This is shorter than either the luminosity lifetime (11 h for D0) or the proton beam lifetime (70 h). It may have corresponded to some sort of halo lifetime. The time dependence was folded in for the analysis.

The effects of leading and trailing satellite buckets were included but additional small terms associated with crossings upstream and downstream of the colliding points were not. The corrections to just using the product of the main bunch populations were less than 3%. The calculated bunch luminosity was then

$$L_{pa} = K I_p I_a A_p A_a = K I_p I_a L_{geo}.$$  \hspace{1cm} (1)

where $K$ is a constant to normalize to the measured luminosities, $A_p$ is the area of the proton beam (assumed to be $\pi \sigma_{ps} \sigma_{ph}$), and $A_a$ is the area of the antiproton beam. $A$ is the overlap area and is calculated using the smallest dimensions of either of the two beams. $L_{geo}$ is the geometric part of the luminosity so that $L_{geo} = A/A_p A_a$ in mm$^{-2}$.

The bunch luminosities were also measured for the D0 cases. These measured luminosities, $L_m$, are given in Table V in units of $10^{-30}$ cm$^{-2}$ s$^{-1}$. Values for $L_{geo}$ are found by multiplying the bunch populations (given in units of $10^9$ particles) in Table V by the relevant beam

| TABLE IV. Bunches colliding at B0 (CDF) and D0. The notation P36·A12 means that proton bunch 36 was colliding with antiproton bunch 12. |
|---|---|
| | B0 (CDF) | D0 |
| P13·A1 | P25·A1 |
| P17·A5 | P29·A5 |
| P24·A12 | P36·A12 |

<table>
<thead>
<tr>
<th>Colliding bunches</th>
<th>$I_p$</th>
<th>$I_a$</th>
<th>$I_p I_a$</th>
<th>$L_{geo}$</th>
<th>$L_{pa}$</th>
<th>$L_m$</th>
</tr>
</thead>
<tbody>
<tr>
<td>P13·A1</td>
<td>54.6</td>
<td>42.5</td>
<td>2364</td>
<td>1.445</td>
<td>0.457</td>
<td></td>
</tr>
<tr>
<td>P17·A5</td>
<td>45.1</td>
<td>41.9</td>
<td>1934</td>
<td>1.308</td>
<td>0.339</td>
<td></td>
</tr>
<tr>
<td>P24·A12</td>
<td>58.6</td>
<td>44.6</td>
<td>2636</td>
<td>1.238</td>
<td>0.437</td>
<td></td>
</tr>
<tr>
<td>P25·A1</td>
<td>29.3</td>
<td>42.5</td>
<td>1273</td>
<td>0.713</td>
<td>0.122</td>
<td>0.132</td>
</tr>
<tr>
<td>P29·A5</td>
<td>70.9</td>
<td>41.9</td>
<td>2995</td>
<td>1.330</td>
<td>0.534</td>
<td>0.494</td>
</tr>
<tr>
<td>P36·A12</td>
<td>39.6</td>
<td>44.6</td>
<td>1822</td>
<td>1.286</td>
<td>0.313</td>
<td>0.309</td>
</tr>
</tbody>
</table>
sizes. \( K \) was determined by averaging the three ratios of the measured luminosities divided by \( L_a I_p I_q \) to give \( K = 1.338 \times 10^{-4} \). The calculated bunch luminosities (\( L_{pa} \)) are also given in Table V. The measured and calculated D0 luminosities (bunches P25-A1, P29-A5, P36-A12) agree quite well. The bunch with the largest difference between the calculated and measured luminosities was P25-A1 where the proton beam dimensions were 30% larger and the current was down by 45%. Note that there was a wide spread in the luminosities of the different bunches.

The count rate difference between colliding and noncolliding buckets is illustrated in Fig. 23. The measured count rates are compared to calculated rates based on luminosity plus an averaged background (see next paragraphs). Measured count rates are shown as histograms with the widths of the gates. Colliding cases are shown as solid histograms while proton-only cases are dashed. [Proton bunches P14 (set 1) and P26 (set 2) were nominally out of time but subsequently were found to overlap colliding buckets.] Since set 1 used a gate that covered three buckets, two of which were colliding, the rates for set 1 were roughly twice as large as set 2. The difference between colliding and noncolliding buckets is clearly visible in Fig. 23.

The time dependent “background” was found by averaging the measured rates of the noncolliding bunches for set 1 (\( B_{1av} = 4282/s \)) and for set 2 (\( B_{2av} = 2723/s \)) extrapolated to an arbitrary \( t_0 \) (30 min before the start of the first set). The measured ratio for \( B_1/B_2 \) is 1.57 while the ratio was expected to be 1.65, because set 1 had three buckets within the gate rather than one for set 2, but the rate had been increased by 1.82 when the crystal was moved in for set 2.

To investigate rate dependence on luminosity the measured background-subtracted, time-normalized extraction rates (\( r = t_0 \)) are plotted against \( L_{pa} \) in Fig. 24. Measured values for set 2 are divided by 1.82 to account for the fact that the rates rose when the crystal was moved in. A fit constrained to go through the origin gives

\[
C/(s) = (0.269 \pm 0.034) \times 10^{-25} \times L_{pa},
\]

where \( L_{pa} \) is in units of \( \text{cm}^{-2}\text{s}^{-1} \) and the rate is based on the crystal to beam separation of 5.5 mm. All of the available information was used. The correlation coefficient is \( r^2 = 0.55 \). While this is not an impressive fit it does suggest that the expected count rate above the background is proportional to luminosity. To the extent the data permit concrete analysis, the contribution of D0 and B0 to the extracted rate seem to have been the same. This formula was used to determine the calculated rates in Fig. 23. The appropriate luminosity was substituted and the background rate was added. Instantaneous values were used for the calculated rates (rather than rates extrapolated to \( t_0 \)) so that count rates on the same bucket measured at two different times have different calculated values in Fig. 23.

Luminous bunches increased the rate substantially. Based on the fit in Fig. 24 [Eq. (2)] a net bunch luminosity of \( 0.5 \times 10^{30} \text{cm}^{-2}\text{s}^{-1} \) gave a luminosity on/off ratio of 4.1. The fitted measured count rate (less background)

![Image](http://example.com/image1.png)  
**FIG. 23.** Illustration of the effect of colliding bunches on count rates for set 1 (CDF and D0 collisions combined) and set 2 (see text). Histograms are measured rates while dots are calculated based on bunch luminosities and a smoothed background. The histogram width is the gate length. The small open circles on the baselines indicate the times of unmeasured bunches. The vertical axis for set 2 is halved because only one bunch was counted. Numbers above a histogram indicate the proton bunch or bunches.

![Image](http://example.com/image2.png)  
**FIG. 24.** Measured, background-subtracted extraction rates normalized to \( t = 0 \) versus luminosity. The line is a fit to the data.
for that luminosity determined from Eq. (2) is 13 300/s. One way to quantify the luminosity on-off ratio is to ask how far the goniometer would have had to be moved in to match a nonluminous bunch to the original luminous rate.

Increasing the nonluminous count rate by a factor of 4 at $x_g = 2.5$ mm was equivalent to decreasing $x_g$ by 0.4 mm or 0.7σx.

It is also interesting to compare luminosity and rf-driven extraction. This can be done by comparing the ratio of the rate with the driver on to the rate with no driver under the same conditions. As noted in the last paragraph this ratio was 4.1 for $L_{pa} = 0.5 \times 10^{30}$ cm$^{-2}$ s$^{-1}$. In the rf-driven case discussed in Sec. VIII the rate for the finger counter coincidence is $R = 15.2 \times V_r^2 + 22$. A ratio of 4 is obtained for $V_{rf} = 2.1$ V.

In summary, it is clear that luminous bunches produce substantially more extracted beam. A useful study would be an investigation of the actual physical mechanisms that influence the beam growth. It would be interesting to try to relate them to the beam loss rates. Models might be developed using emittance growth and beam lifetime studies undertaken for the SSC and the Large Hadron Collider (LHC).

## X. APPLICATIONS

Multiple pass crystal extraction, first observed at CERN [18], has made crystal extraction very interesting. With multiple passes the nonchanneled beam goes through the crystal many times until it interacts or channels and is extracted. The angular divergence of the extracted beam in the bend direction is small, on the order of the channeling critical angle.

The application of crystal extraction most frequently considered for TeV-range accelerators has been scraping of the halo in a collider to produce parasitic beams in the 1 MHz regime. In E853 a parasitic 120 Khz beam was extracted at C0 without undue background impact on the collider detectors. Parenthetically, the collider loss monitors were set conservatively during E853 and little headroom was allowed for losses.

Crystal extraction can also work for dedicated extraction. While the efficiency is not as good as with an electrostatic septum, it can potentially be well above 50%. Recent Serpukhov studies [13] have found that short “O” shaped crystals with no straight ends and smaller radii of curvature increase the efficiency further, as expected.

With crystals the large bends relative to conventional electrostatic deflection offer intriguing possibilities for applications. For example, crystal extraction has been used with success in the tight lattice at Serpukhov. It could also be used to pack extraction facilities into oversubscribed straight sections at colliders. One ambitious suggestion is the possibility of directing neutrino beams toward cosmic ray facilities well off the plane of an accelerator by steering the extracted protons used to produce the neutrinos [20]. The following subsections discuss TeV extraction and possible charm experiments including magnetic moment measurements.

### A. TeV Extraction at Fermilab

An interesting candidate for crystal extraction is a parasitic collider beam from the Tevatron A0 straight section into the fixed target experimental areas. A 1000 GeV beam would have 25% higher energy than any fixed target beam of the past. The beam could be useful for such projects as LHC development test beams. The spill structure would be uniform without the normal fixed target magnet ramping cycle. The beam-on time would correspond to the “on” time for the collider. The beam could be switched to several different experimental areas. Switching would lessen problems of operating the switchyard above 800 GeV. The beam could also be operated at higher intensities for short periods in a dedicated mode.

For parasitic operation the crystal would operate like the E853 crystal. The principal difference is that a much larger bend angle would be required to avoid obstructions at A0 and to mate with the switchyard beam line.

A possible location for a bent crystal in the Tevatron is just after the last A0 proton kicker magnet as shown in Fig. 25. An illustrative geometry has been discussed in more detail elsewhere [21]. The kicker magnet chain normally kicks the beam into the 10 m long A0 abort absorber [22]. In the illustrative geometry a horizontal bend of 15.7 mrad is required to cross the switchyard beam at PV92 and also to miss the abort dump. A vertical bend of 4.7 mrad is also needed leading to a combined bend of 16.4 mrad. Both bends could be provided by tilting the crystal just as was done with the skew dipole chain for normal fixed target operation. The extraction and transmission efficiency of the extraction crystal would be about 9% based on the Biryukov E853 simulation [3] and other models of the channeling process [23].

For the illustrative model a reasonable place to reconnect with the switchyard beam line is at PV92. This would require a horizontal bend of 7.17 mrad coupled with a downward vertical bend of 2.17 mrad. This could be done with several dipole magnets or a second crystal.

Crystal extracted beam intensity is related to the circulating proton beam loss rate. There is a natural loss rate that occurs due to the beam-beam interaction at the collision points, gas scattering, nonlinearities, and other sources. At the Tevatron collider the beam-beam interaction is the dominant source of loss for present and future luminosities. These natural losses must be controlled by scraping the circulating beam. In fact a scraping crystal could cut the loss rate at the detectors. Such a possibility was discussed for the SSC [24] and has been considered for the Tevatron.
The external beam rate is then a function of the beam loss in the accelerator, the fraction of the beam losses that strike the crystal, the overall extraction and deflection efficiency of the crystal system, and the maximum allowed loss rate at the collider detectors. For E853 the CDF loss limit at their detector was limited to less than 5 Khz with a loss rate of 3.5 kHz without the crystal, and the D0 limit was <1 kHz with a loss rate quite close to that. Six bunches were colliding, the circulating proton beam was $10^{12}$, the proton lifetime was 75 h, the luminosity lifetime was 15 h, and the CDF luminosity was typically $0.5 \times 10^{31}$ cm$^{-2}$s$^{-1}$.

A good extracted rate for E853, which kept the D0 loss within its limit was 0.15 MHz. The extraction efficiency was of the order of 25%, so that 0.6 MHz was incident on the crystal. With the main injector on-line, there are 36 bunches rather than 6 and the proton intensity has increased correspondingly. It is reasonable to expect that the beam incident on a crystal could be 6 MHz. An optimized crystal length of 12.5 cm results in an extraction efficiency of 9%, so that the beam transmitted down the switchyard line would be 0.5 MHz or 0.3 protons per bunch per turn.

This design could be improved in several ways. A germanium crystal [25] with its larger critical angle would help. A smaller crystal bending angle could feed a septum magnet chain such as the Lambertson string no longer needed for collider operation. These two improvements could result in a gain of 5 to 10. Another possibility would be to cool the crystal [26]. This would increase the dechanneling length and improve the extraction efficiency, perhaps by a factor of 2. Finally a prescatterer such as a one-quarter channeling wavelength crystal [27] or an amorphous target [28] might raise the yield by a factor of 2. With these improvements a 5–10 MHz beam is within reach.

There was no evidence of radiation damage in 70 h of operation for E853. An extraction crystal would have to last about 100 times longer. Measurable damage [29] with an effect on channeling occurs at a rate on the order of $10^{20}$ protons/cm$^2$. Assuming the active region of the crystal is 10 μm wide and 0.6 mm high, an extraction crystal should be able to handle on the order of $10^{16}$ particle passes or years of parasitic operation.

### B. A charm experiment using a crystal extracted beam

The possible application of a crystal extracted beam for a fixed target heavy flavor experiment has been explored in some detail for the SSC, the LHC, and the Tevatron [30]. The Fermilab fixed target experiment E771 produced $1.6 \times 10^{9}$ charm pairs during a 30 day run in a 40 MHz beam with a 5% interaction length target. Based on that a 10 MHz parasitic crystal-extracted beam could produce $10^{10}$ charm events in a year. Physics possibilities include observations of mixing in the charm sector and CP violation in $D^0$ decays.

### C. Measuring charm baryon magnetic moments

Charm baryon magnetic moment measurements could provide direct information on the magnetic moment of the charm quark. Short charm lifetimes make such measurements difficult with conventional techniques. With the high effective magnetic fields available in a bent crystal charm moment measurements are conceivable [31]. An experiment at Fermilab [32] used this approach to measure the magnetic moment of the $\Sigma^+$. Optimistically a 6% measurement of the $\Lambda^+$ magnetic moment would require 3000 $\Lambda^+ \rightarrow p + K^- + \pi^+$ events. This would need $4 \times 10^{13}$ protons or about a month of running in a 10 MHz beam. One distinct advantage of a parasitic extraction beam for the experiment would be the lower proton rate on target because the beam live time would be 100% rather than the normal 33% for the Tevatron fixed target program.
XI. SUMMARY

E853 has demonstrated that useful TeV-scale beams can be extracted from a superconducting accelerator with a bent crystal in the course of collider operation. An important aspect of this is multipass extraction, which substantially increases the efficiency of the process. A significant luminosity-generated halo created by normal collider operation was observed and extracted. This was done without unduly affecting the backgrounds at the collider detectors. The experiment was able to study both luminosity-driven extraction and multipass effects in enough detail to confidently apply the technique to real situations.

Extraction efficiency was studied in some detail but proven rather hard to measure accurately during a tightly packed accelerator schedule where much of the E853 running was parasitic. Nevertheless, it was found that the extraction efficiency is consistent with the Biryukov simulation and that the simulation can be used to extrapolate to future beam designs.

Time dependent effects in the experiment have provided interesting insights into several crystal extraction and accelerator beam halo phenomena.

In the kick mode the major time structure was due to accelerator beam dynamics. The turn-to-turn microstructure was sensitive to the accelerator tune and more indicative of tune changes than channeling phenomena. Following an initial decay with a time constant on the order of 1 ms the extraction signal was almost flat and then dropped in the 30 ms region. Small, longer-term extraction pulses occurred out to 5 s. Kick mode extraction was reasonably modeled by the simulation programs except for the long-term persistence and the fact that so-called wrong side turns came into equilibrium with right side turns after a time constant comparable to the initial fall time for right side buckets. These effects may have been due to nonlinearities in the accelerator.

The time for an extracted signal to appear in the kick mode for a misaligned crystal was also studied. This possibility arose because of multipasses through the crystal and the associated multiple scattering. The times are consistent with a simulation and also with a simple picture of the process based on multiple scattering.

Other E853 observations related to the character of the circulating accelerator beam halo. Retracting the crystal or a collimator shed light on the diffusion rate of the halo. This rate was related to the beam halo phase space density and nonlinear effects in the accelerator system. Typically a 200 µm crystal pullout dropped the extraction rate by a factor of 4 after which it increased with a time constant of several minutes. Based on this information it is difficult to speculate on how halo diffusion depends on the pullout distance.

Related halo information was provided by measurements of the number of kicks required to move the edge of the beam out to the crystal. Typically with a 10 kV kick it took five to seven kicks to grow the beam.

When the crystal was moved in the rate rose instantly and then relaxed in less than a minute to an equilibrium point with a much longer decay period. After the initial rapid fall the characteristic rates for luminosity on-off and the proton-only cases typically dropped with a 1.5 h decay constant.

Using the kick mode little evidence was found for oscillations and modulations beyond some indication of a weak modulation with a period in the range of 30–50 ms. This modulation could have been due to any of several effects including subharmonics of the line frequency or synchrotron oscillations.

Use of transverse white rf noise from a horizontal damper at F11 increased the extraction rate dramatically. Little interesting was learned about time dependent effects from the damper studies. Equilibrium was reached in less than 10 s when the damper was turned on or off.

This experiment demonstrated luminosity-driven extraction for the first time by simultaneously monitoring colliding and noncolliding proton bunches. The extraction rate was found to be proportional to the luminosity. The luminosity on/luminosity off ratio increased by a factor of 4 for a bunch luminosity of 0.5 × 10^{30} cm^{-2}s^{-1}. This was equivalent to decreasing the goniometer distance from the beam by 0.4 mm or 0.7 σ_{x}. The impacts of the luminous regions were similar to the effect of the rf noise source at F11. An rf noise signal of 2.1 V (rms) was equivalent to a bunch luminosity of 0.5 × 10^{30} cm^{-2}s^{-1}.

One potential application for crystal extraction is the construction of a parasitic collider beam from the Tevatron. A 1000 GeV beam into the fixed target areas would have 25% higher energy than any earlier beam. For an optimized geometry with 6 MHz lost on the crystal a 0.5 MHz beam would be transmitted to a fixed target area. With improvements a 5 to 10 MHz beam would be possible. This beam could be used for heavy flavor experiments such as observations of mixing in the charm sector and CP violation in D^0 decays. Another possibility would employ a bent crystal for measurements of charm baryon magnetic moments.

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